



Deoxygenation rate, reaeration and potential for self-purification of a small tropical urban stream

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Joao Paulo Cunha de Menezes* ; Ricardo Parreira Bittencourt;
Matheus De Sá Farias; Italoema Pinheiro Bello;
Luiz Fernando Coutinho de Oliveira; Ronaldo Fia

Universidade Federal Lavras (UFLA), Lavras, MG, Brasil
Departamento de Engenharia

*Corresponding author: e-mail: jpaulo_bio@hotmail.com,
ricardoparreira.rp@gmail.com, matheus_desafs@hotmail.com,
italoemapb@hotmail.com, coutinho@deg.ufla.br, ronaldofia@prg.ufla.br

ABSTRACT

Mathematical models used to simulate the water quality and the processes of self-purification of water bodies are important tools to support effective water resource management. The objective of this study was to evaluate the impact of organic pollution on water quality and the assimilative capacity of organic matter in the Ribeirão Vermelho stream situated in the city of Lavras in Minas Gerais. The deoxygenation rate (K_1) and reaeration (K_2) were determined and tested in three segments of the Ribeirão Vermelho over two seasons (summer and winter). The purification process simulation was performed using the Streeter-Phelps model. The highest K_1 and K_2 values occurred during the winter period which was characterized by lower flows. Simulation of the dissolved oxygen profile and biological oxygen demand fitted the model well, indicating the prevalence of carbonaceous deoxygenation due to nitrification and also demonstrating the importance of natural reaeration as part of the purification process. Different response was observed during the winter, in which the high primary productivity values stood in the reaeration process stream. Biological oxygen demand values did not meet the limits recommended by the Resolution of the Ministry of the Environment 357/2005 throughout the river system and the entire study period. In conclusion, the Ribeirão Vermelho is unable to self-purify along its entire length, and water quality is influenced by effluent discharge which intensifies degradation.

Keywords: effluent release, Streeter Phelps models, water quality.

Coeficiente de desoxigenação, reaeração e potencial de auto purificação de um ribeirão urbano

RESUMO

Os modelos matemáticos utilizados para simular a qualidade da água e o processo de autodepuração de corpos d'água são importantes ferramentas de auxílio à gestão dos recursos hídricos. Assim, o objetivo deste trabalho foi avaliar o impacto da poluição orgânica na qualidade da água e a capacidade de assimilação da matéria orgânica no Ribeirão Vermelho.

Para essa finalidade, foi desenvolvido e testados os coeficientes de desoxigenação (K_1) e reaeração (K_2), em três trechos e em dois períodos distintos (verão e inverno). Os maiores valores de K_1 e K_2 foram obtidos durante o inverno, onde foram registrados as menores vazões. A simulação do processo de autodepuração foi realizada com o uso do modelo de Streeter-Phelps. A simulação do perfil de OD e DBO no verão apresentou calibração aceitável, tendo em vista a otimização dos coeficientes, evidenciando a prevalência da desoxigenação por demanda carbonácea sobre a nitrificação e a importância da reaeração natural no processo de autodepuração. Comportamento diferente foi observado no inverno, no qual os altos valores de produtividades sobressaíram no processo de reaeração no ribeirão. Apenas o parâmetro demanda bioquímica de oxigênio não respeitou os limites preconizados pela Resolução do Ministério do Meio Ambiente 357/2005, tendo ficado em toda a extensão do rio e, em ambos períodos, fora da regulamentação. Desta forma, conclui-se que o Ribeirão Vermelho não consegue se auto depurar ao longo de sua extensão até a foz, tendo a qualidade de suas águas influenciadas por lançamentos de efluentes que intensifica o processo de degradação do rio.

Palavras-chave: lançamento de efluentes, modelo qualidade de água, Streeter Phelps.

1. INTRODUCTION

Rivers play an important role in the uptake and transport of industrial, municipal effluents and organic loading caused by runoff from agricultural fields, roads, and streets. Leaching and direct effluent discharge are primary sources of water pollution (Shrestha and Kazama, 2007). This problem is exacerbated when the purifying capacity of river systems is low in relation to the received contaminants.

Water self-purification is a complex process involving physical, chemical and biological processes that occur simultaneously, allowing a river can recover its natural state over a certain distance (Vagnetti et al., 2003; Demars and Manson, 2013). Depuration comprises different mechanisms such as dilution, sedimentation, reaeration, adsorption, absorption, and chemical and biological reactions, and can be evaluated by the same mathematical model (Bahadur et al., 2013, González et al., 2014). Water quality models are essential tools for the development of planning and management measures for water resources in river basins (Panagopoulos et al., 2012).

The precursor of more contemporary water quality models was proposed by Streeter and Phelps (1925), and was applied in a study on the Ohio River to increase the efficiency of actions to control pollution. The Streeter-Phelps model has resulted in the subsequent development of numerous numerical models used in computer applications, such as: QUAL-I, II and E (Fischer, 1995), QUAL-2K (Chapra et al., 2006), among others (Bahadur et al., 2013). These models, derived from classical Streeter-Phelps equations, have been widely used not only in to assess water quality, but also to predict damage resulting from the implementation of water resources management measures.

The Streeter-Phelps model describes “as oxygen demand decreases in a river or stream along a certain distance by degradation of biochemical oxygen demand. Changes in the oxygen content of polluted waters over time can be studied by using the dissolved oxygen sag curve” (Von-Sperling, 2014). “This differential equation states that the total change in oxygen deficit is equal to the difference between the two rates of deoxygenation (K_1) and reaeration (K_2) at any time” (Streeter and Phelps; 1925, Von-Sperling, 2014).

Estimation of K_1 and K_2 parameters is important for selecting a solution curve that best represents a real system. However, there is no method available to determine values that fit precisely to the reality of a given water body. Reaeration coefficients vary widely due

to their dependence on air-water interface turbulence making them complex and difficult to accurately measure. Several studies give methods to estimate K_1 and K_2 that provide reasonable approximations within predefined limits. However, due to the non-linearity nature of these coefficients, there is no formula for generic cases (Raymond et al., 2012; Cox, 2003; Haider et al., 2013; Benson et al., 2014).

Nowadays there is a strong interest in integrated approaches to the management of urban basins, since these systems are subject to a wide range of environmental problems. The primary objective of this study was to assess the impact of organic pollution on river water quality and the water self-purification capacity in the Ribeirão Vermelho Basin.

2. MATERIAL AND METHODS

Located in the Greater Region South of Minas Gerais, the river basin of the Ribeirão Vermelho, a tributary of the Rio Grande, includes the city of Lavras (Figure 1). Both the source and main tributaries of the Ribeirão Vermelho are situated in the urban area of the city of Lavras which has a population of approximately 90,000 inhabitants (IBGE, 2010). After flowing for approximately 15 km, the Ribeirão Vermelho flows into the Rio Grande, one of the main tributaries in the Paraná River Basin. Although most of the area of the Ribeirão Vermelho Basin has sewerage, some areas have septic tank systems and also illegal sewerage that discharges directly into the watercourse.

According to the Köppen classification, the climate where the city of Lavras is situated is classified as Cwb, which describes a rainy temperate (mesothermal) climate with a dry winter and a rainy summer. The region is subtropical with an annual temperature of approx. 19.3°C (maximum of 21.3°C 15.1°C). The normal annual rainfall is approximately 1,530 mm (Alvares et al., 2013).

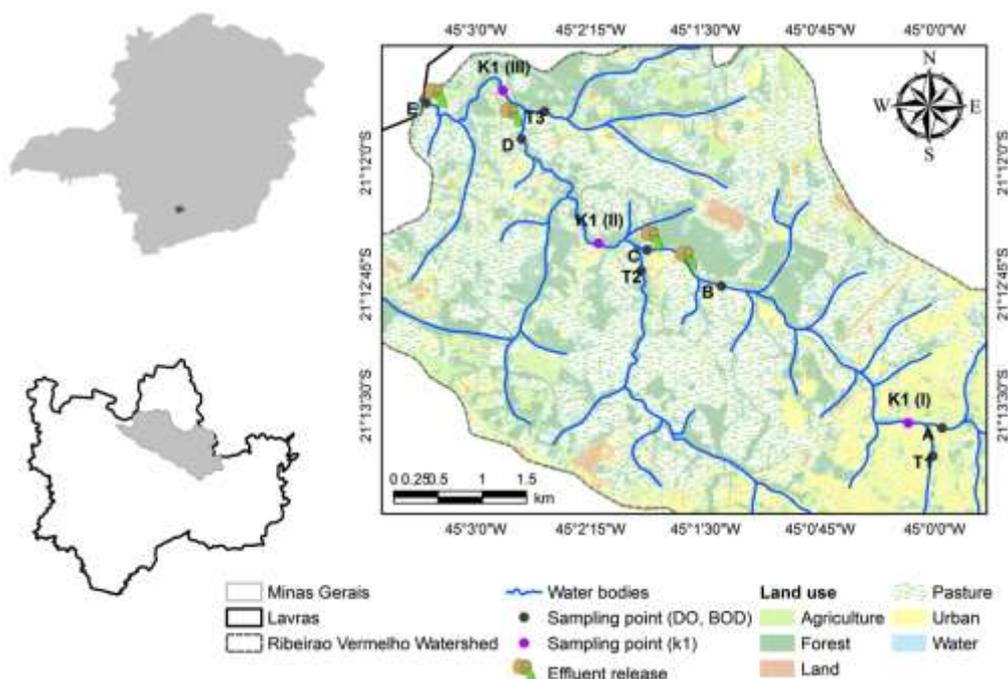


Figure 1. Location of the Ribeirão Vermelho River Basin, with detail of land use and the sampling points for the Streeter-Phelps model input parameters and effluent discharges.

The Vermelho Ribeirão stream was divided into three sections for the simulation study of the purification process, namely: section I, from 0 to 4.76 km; II, from 4.76 to 7.19 km and

III, from 7.19 to 8.65 km (Figure 1). The criterion for defining and creating each section was based on the hydraulic characteristics of the river, the location of polluting sources and confluence to the stream.

Four field campaigns (April-October, 2014), in two periods (summer and winter) were carried out to determine the input variables of the self-purification model at 11 sampling stations with different degrees of anthropogenic impact and potential sources of pollution (Figure 1). Dissolved oxygen (DO) levels and biochemical oxygen demand (BOD) were measured at eight sampling stations and the remaining three sampling stations after each mixture of affluent). Water samples were collected at 3 points after mixing with the main river affluent (Figure 1) to determine the deoxygenation coefficient (K_1). Sampling was carried out manually by collecting near the water surface, due to the shallow water depth in the study area. Analyses were carried out in Water Analysis Laboratory of the Environmental Engineering and Sanitary Engineering at Department of the Federal University of Lavras.

Water temperature was measured *in situ* using a mercury thermometer, and the altitude of each point was obtained using a handheld GPS (Global Positioning System). Both DO and BOD were determined using the iodometric method (APHA et al., 2005). The BOD was determined on 20 consecutive days in order to estimate the rate of deoxygenation and calculate K_1 values as described by von Sperling (2014). After evaluating the BOD, a theoretical curve was constructed using the non-linear regression method to set multiple values of sampling time points and BOD. Therefore, estimated K_1 values were obtained from the deoxygenation rate. The reaeration coefficient (K_2) was obtained using the Microsoft Excel Solver[®] tool in replacing Equation 4, the input data (temperature, altitude location, the mixing point DO, BOD, speed, K_1 , and the distance DO concentration at the end of excerpt).

Water flow was estimated using the hydrometric method. Depth and average flow velocity was measured with the aid of a flow meter at cross sections situated at the upstream and downstream end of each designated stretch; flow was assessed using a continuity equation. The input data was used to model the dissolved oxygen using the classic version proposed by Streeter and Phelps (1925).

$$C(t) = S_C - \left[\frac{K_1 \cdot L_0}{K_2 \cdot k_1} \cdot \left(e^{-\frac{K_1}{v} \cdot t} - e^{-\frac{K_2}{v} \cdot t} \right) + (S_C - C_0) \cdot e^{-\frac{K_2}{v} \cdot t} \right] \quad (1)$$

where:

L_0 = final BOD (mg L^{-1});

C_0 = initial concentration of the river DO (mg L^{-1});

v = mean velocity of water flow (m s^{-1});

t = time (days);

K_1 and K_2 = coefficients of reaeration and deoxygenation, respectively (day^{-1});

$C(t)$ = concentration of dissolved oxygen (DO) in time (mg L^{-1});

S_C = DO saturation concentration (mg L^{-1}).

Water quality standards were drawn from CONAMA, Resolution No. 357/2005 (CONAMA, 2005) to assess compliance with environmental legislation for the Ribeirão Vermelho (class 2).

3. RESULTS AND DISCUSSION

The average flow of the Ribeirão Vermelho increased along the river over the study period, ranging from 0.26 to 0.43 $\text{m}^3 \text{s}^{-1}$ during the summer and from 0.09 to 0.25 $\text{m}^3 \text{s}^{-1}$

during the winter. DO levels increased along with the values of biological oxygen demand (BOD) (Figure 2).

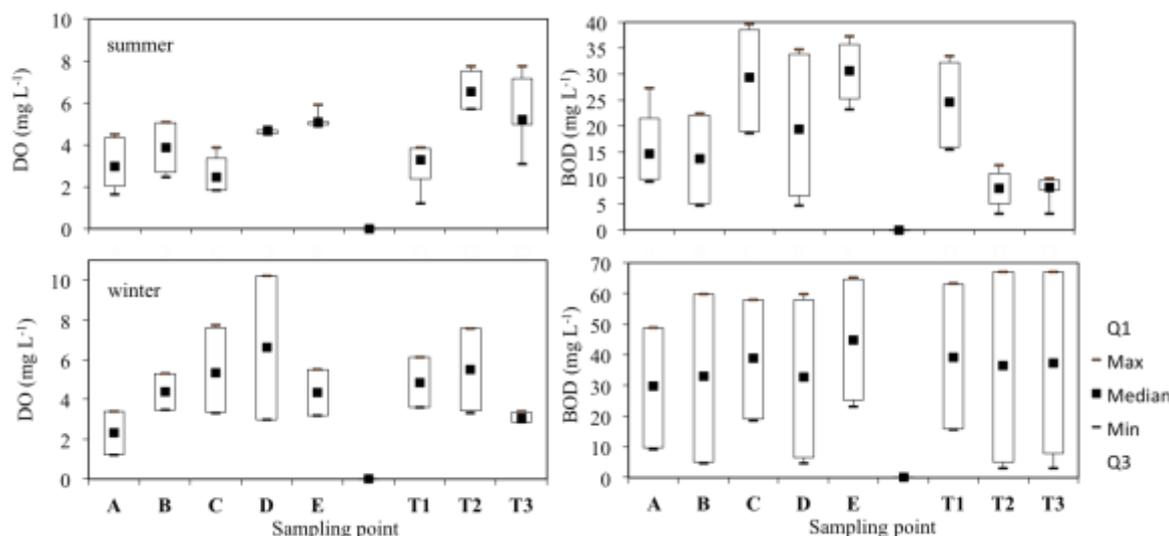


Figure 2. Spatiotemporal variation of Dissolved Oxygen (DO) and Biological Oxygen Demand (BOD) along the Ribeirão Vermelho.

The higher winter DO levels reflect higher primary productivity levels and eutrophication of the river. Although Figure 2 shows a purification trend, BOD concentrations did not fall along the river, possibly due to agro-industrial waste discharge senescence of algae in the water column of the river. Other sources of organic matter also influenced the process due to the water quality of the Ribeirão Vermelho during the winter period (Figure 2).

According to the River Continuum Theory, various processes and patterns of the river ecosystem are changing along the river as conditions change (Vannote et al., 1980; Bowes et al., 2003). Biogeochemical processes that occur throughout the river basin and hydrological pulses affect water quality along the river continuously (Magnuszewski et al., 2007; Kiedrzyńska et al., 2008). Although sewerage infrastructures serve a large percentage of the rural enterprises, some areas have septic tank systems and illegal piping connections discharging untreated sewage directly into the stream, changing the river purifications patterns.

The deoxygenation rate constant (K_1) was calculated from BOD data and adjusted in accordance with the corresponding curves using the method proposed by Thomas (1950), as well as temperature adjustment proposed by Tebbut (1998). The R^2 coefficients were very close to unity, indicating a close association of estimated and observed data (Table 1). Sections I and III of the study area showed a higher K_1 values in summer and winter period (Table 1).

The highest summer K_1 values may be due to the higher concentration of organic matter carried from the river because of runoff while maintaining a contribution of gross organic matter in the stream. According to Almeida (2006), K_1 varies with temperature, influencing microbial metabolism, the composition and concentration of the organic material from the source of pollution. In order to quantify the K_1 coefficient at different times of the year on the river Turvo Sujo in Minas Gerais, Barros et al. (2011) observed average summer K_1 values of 0.14 d^{-1} , which was slightly higher than the average K_1 value for the winter period (0.12 d^{-1}) which, according to the author, was due to the organic load of the rainfall runoff into the watercourse, corroborating the results obtained in this work. The Ribeirão Vermelho K_1 values were similar to values found in the technical literature, and they were classified as

clean water or secondary effluent (Fair et al., 1973; Arceivala, 1981; Thomann and Mueller, 1987; Tebbut, 1988; Chapra, 1997; Almeida, 2006; Von-Sperling, 2007; Formentini, 2010; Santos et al., 2011; Von-Sperling, 2014).

Table 1. Mean and standard deviation values of the deoxygenation coefficient (K_1) and coefficient of reaeration (K_2) at each sampling section, with its BOD_5 and the last oxygen demand (L_0).

Section	Q ($m^3 s^{-1}$)	BOD_5 ($mg L^{-1}$)	K_1 (d^{-1})	R^2	L_0 ($mg L^{-1}$)	K_2 (d^{-1})
summer						
I	0.26	24.5 ± 3.11	0.13 ± 0.01	0.99	72.1 ± 4.5	4.0
II	0.39	23.9 ± 5.26	0.08 ± 0.04	0.98	100.7 ± 8.1	2.5
III	0.43	24.9 ± 6.92	0.12 ± 0.01	0.98	84.5 ± 15.7	7.4
winter						
I	0.09	24.9 ± 2.71	0.09 ± 0.04	0.99	90.4 ± 17.7	5.3
II	0.18	30.4 ± 3.45	0.07 ± 0.05	0.98	171.8 ± 68.7	14.58
III	0.25	41.6 ± 4.20	0.15 ± 0.05	0.98	101.5 ± 3.7	*

*in Section III during the winter period, it was not possible to determine the methodology used by K_2 due to excess oxygen present in the liquid mass due to the high primary productivity of the river.

The last oxygen demand was higher in periods of low flow, when the concentration of pollutants was higher. Barros et al. (2011) evaluating the oxygen balance in the river Turvo Sujo in different seasons. In their study, they also observed this pattern, noting that the water samples had lower K_1 values and a slower stabilization rate of organic matter, resulting in a high L_0 . In contrast, samples with higher values of deoxygenation degraded organic matter more rapidly.

According to von-Sperling (2014), the importance of the coefficient K_1 and BOD a relativity concept may be considered when two different samples have the same value as BOD_5 , which apparently could lead to the conclusion that the impact in terms of dissolved oxygen uptake is the same in both situations. However, BOD values varied daily over the sampling periods in the Ribeirão Vermelho (Figure 3) with the exception of the fifth day. This is due to different deoxygenation rates in the two samples, emphasizing that the interpretation of BOD data must always be linked to the concept of deoxygenation ratio and therefore the oxidation rate of the organic matter (Von-Sperling, 2014).

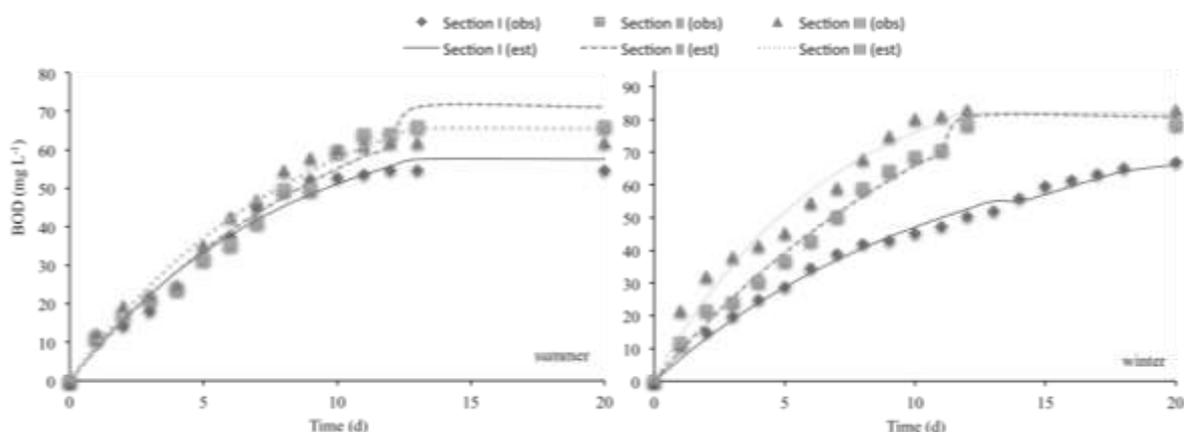


Figure 3. Curve progression of the BOD over time in water samples collected in three different stretches of the Ribeirão Vermelho in two periods (summer and winter).

Estimated values of the reaeration coefficient for the three segments of the Ribeirão Vermelho, with different hydrodynamic conditions in both periods evaluated are shown in Table 1. K_2 values are normally obtained using empirical models. However, this study used an inverse method using Equation 1 to obtain K_2 values by inserting the input data and the oxygen concentration at a certain time in order to minimize the sum of squares of deviation.

The highest K_2 values were recorded during the low flow winter period when the shallower depth was possibly an influential factor. According to Von-Sperling (2014) bodies of shallower water tend to have higher coefficient of reaeration, due to ease of mixing across the depth profile and greater surface turbulence. Haider et al. (2013) evaluated predictive models of reaeration coefficients in a river in Pakistan and observed that K_2 may vary significantly based on the hydrodynamic conditions of the river and the applied model.

The Ribeirão Vermelho purification capacity, considering the real contribution of its tributaries and seasonal patterns, was analyzed using the Streeter and Phelps Model (1925) and quantitative and qualitative data measured on site (Figure 2 and Table 1). The results show a good fit of the data to the model in both periods (Figure 4).

With the exception of the summer, the evolution of the DO concentration as a function of distance along the study site shows a tendency for the Ribeirão Vermelho to meet the proposed level for bodies of water in Class 2 condition, as determined by CONAMA Resolution No. 357/2005 (CONAMA, 2005). However, in the winter, the majority of sampling sites had high dissolved oxygen levels due to excess oxygen produced by the high productivity of algae present rather than the river's capacity to assimilate organic matter. Pollution from agropastoral activities resulted in $BOD_{5,20^\circ C}$ exceeding the regulatory maximum value of 5.0 mg L^{-1} . This trend is due to frequent interruptions in the river purification process as a result of direct discharge which makes the prediction of system recovery a difficult task.

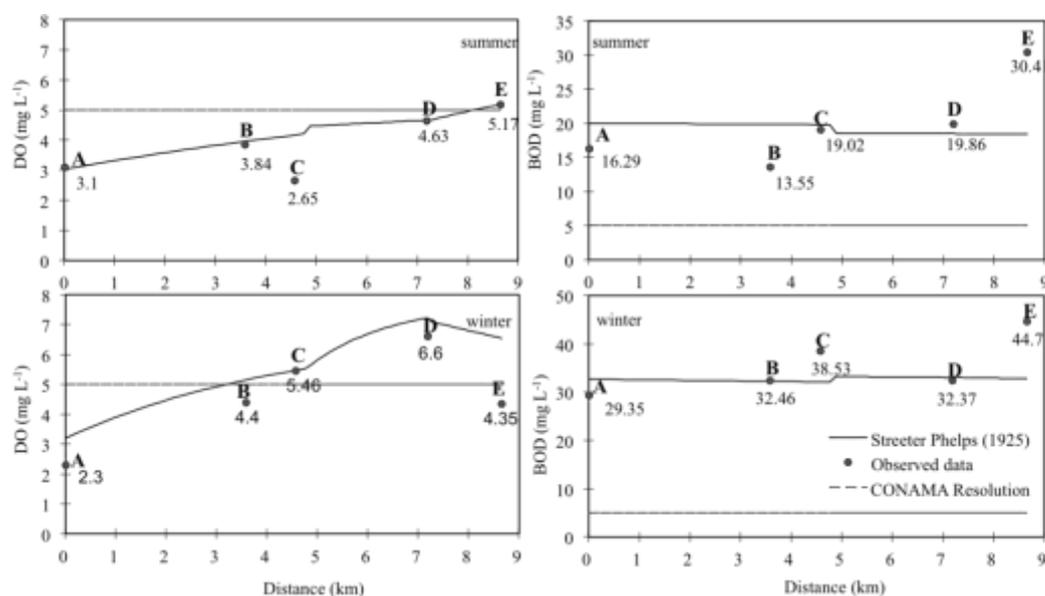


Figure 4. Spatial variation of average concentrations of dissolved oxygen (DO) and biological oxygen demand (BOD) observed and modeled by the equation proposed by Streeter and Phelps (1925) in Ribeirão Vermelho.

4. CONCLUSION

The highest values found for the K_1 parameter occurred during the winter when flow levels were low in the studied sections and organic loading was greater.

The estimation of K_2 by means of the inverse solution equation, proposed by Streeter-Phelps, fits well to the data obtained in this study of the Ribeirão Vermelho sections.

The use of the Streeter-Phelps purification model was consistent with the experimental samples taken from stream. The observed concordance between the model and the experimental data is due to the fact that the point source and the kinetic coefficients of deoxygenation (K_1) and reoxygenation (K_2) were obtained in the field and used as calibration parameters.

Analysis of timeline concentrations of DO and BOD revealed a significant negative environmental impact in Ribeirão Vermelho, caused by the release of organic matter from agro-industrial effluents and municipal wastewater.

This study contributes towards a better understanding of pollution dynamics in the Ribeirão Vermelho and draws attention to potential environmental problems that may occur. Also it warns about the problems caused by effluent discharges into the Ribeirão Vermelho, since from this study it was possible to support reliable models and improve the management of water resources.

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